## AS Further Mathematics Unit 2: Further Statistics A General instructions for marking GCE Mathematics

1. The mark scheme should be applied precisely and no departure made from it. Marks should be awarded directly as indicated and no further subdivision made.
2. Marking Abbreviations

The following may be used in marking schemes or in the marking of scripts to indicate reasons for the marks awarded.

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cao = correct answer only
MR = misread
PA = premature approximation
bod = benefit of doubt
oe = or equivalent
si = seen or implied
ISW = ignore subsequent working
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F.T. $=$ follow through ( $\boldsymbol{\imath}$ indicates correct working following an error and
indicates a further error has been made)

Anything given in brackets in the marking scheme is expected but, not required, to gain credit.
3. Premature Approximation

A candidate who approximates prematurely and then proceeds correctly to a final answer loses 1 mark as directed by the Principal Examiner.
4. Misreads

When the data of a question is misread in such a way as not to alter the aim or difficulty of a question, follow through the working and allot marks for the candidates' answers as on the scheme using the new data.
This is only applicable if a wrong value, is used consistently throughout a solution; if the correct value appears anywhere, the solution is not classed as MR (but may, of course, still earn other marks).
5. Marking codes

- 'M' marks are awarded for any correct method applied to appropriate working, even though a numerical error may be involved. Once earned they cannot be lost.
- ' $m$ ' marks are dependant method marks. They are only given if the relevant previous ' $M$ ' mark has been earned.
- 'A' marks are given for a numerically correct stage, for a correct result or for an answer lying within a specified range. They are only given if the relevant $\mathrm{M} / \mathrm{m}$ mark has been earned either explicitly or by inference from the correct answer.
- 'B' marks are independent of method and are usually awarded for an accurate result or statement.
- 'S' marks are awarded for strategy
- 'E' marks are awarded for explanation
- 'U' marks are awarded for units
- 'P' marks are awarded for plotting points
- 'C' marks are awarded for drawing curves


## AS Further Mathematics Unit 2: Further Statistics A

## Solutions and Mark Scheme

| $\begin{aligned} & \text { Qu. } \\ & \text { No. } \end{aligned}$ | Solution | Mark | AO | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 1.(a) <br> (b) | $\begin{aligned} E(W) & =E(X) E(Y)=168 \\ E\left(X^{2}\right) & =(E(X))^{2}+\operatorname{Var}(X) \\ & =221 \\ E\left(Y^{2}\right) & =153 \\ \operatorname{Var}(W) & =E\left(W^{2}\right)-[E(W)]^{2} \\ & =E\left(X^{2}\right) E\left(Y^{2}\right)-(E(X) E(Y))^{2} \\ & =221 \times 153-168^{2}(=5589) \\ \mathrm{SD} & =74.8(74.75961 \ldots) \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & {[7]} \end{aligned}$ | $\begin{aligned} & \mathrm{AO} 1 \\ & \mathrm{AO} 1 \\ & \mathrm{AO} 1 \\ & \mathrm{AO} 1 \\ & \mathrm{AO} 3 \\ & \mathrm{AO} 1 \\ & \mathrm{AO} 1 \end{aligned}$ |  |
| $2(a)$ | $\begin{aligned} E(T)= & \frac{1}{2500} \int_{0}^{10} t^{2}\left(100-t^{2}\right) \mathrm{d} t \\ & =\frac{1}{2500}\left[\frac{100 t^{3}}{3}-\frac{t^{5}}{5}\right]_{0}^{10} \\ & =5.33(333 \ldots) \end{aligned}$ | M1 <br> A1 <br> A1 | $\begin{aligned} & \mathrm{AO} 3 \\ & \mathrm{AO} 1 \\ & \mathrm{AO} 1 \end{aligned}$ |  |
| (b)(i) | $\begin{aligned} & F(t)=\frac{1}{2500} \int_{0}^{t} u\left(100-u^{2}\right) \mathrm{d} u \\ &=\frac{1}{2500}\left[50 u^{2}-\frac{u^{4}}{4}\right]_{0}^{t} \\ &=\frac{1}{2500}\left(50 t^{2}-\frac{t^{4}}{4}\right)(\mathrm{fc} \\ &0 \leq t \leq 10) \\ &=1 \text { for } t>10 \\ &(F(t)=0 \text { for } t<0) \end{aligned}$ | M1 <br> A1 <br> A1 <br> B1 | AO3 <br> AO1 <br> AO1 <br> AO1 | Allow omission of $t<0$ |
| (ii) | $\begin{aligned} P(T>5)=1- & F(5) \\ & =0.563 \quad(0.5625) \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | $\begin{aligned} & \mathrm{AO} 3 \\ & \mathrm{AO} 1 \end{aligned}$ |  |
| (iii) | The median $m$ satisfies $F(m)=0.5$ $\begin{gathered} m^{4}-200 m^{2}+5000=0 \\ m^{2}=\frac{200 \pm \sqrt{40000-20000}}{2} \\ (=29.289 \ldots) \\ m=5.41(1961 \ldots) \end{gathered}$ | M1 <br> A1 <br> A1 <br> A1 <br> [13] | AO3 <br> AO3 <br> AO1 <br> AO1 |  |




| $\begin{aligned} & \text { Qu. } \\ & \text { No. } \end{aligned}$ | Solution |  |  |  | Mark | AO | Notes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7(a)(i) | $\mathrm{H}_{0}$ : There is no association between parents knowing their child's social media passwords and age of child <br> $\mathrm{H}_{1}$ : There is an association between parents knowing their child's social media passwords and age of child |  |  |  | B1 | AO3 | Or $\mathrm{H}_{0}$ : Parents knowing their child's social media passwords is independent of age $\mathrm{H}_{1}$ : Parents knowing their child's social media passwords is not independent of age |
| (ii) | Expected values |  |  |  |  |  |  |
|  | Parent <br> knows <br> password | 13 | 14 | 15 |  |  |  |
|  | Yes | 62.79 79.21 | 78.71 | 76.50 |  |  |  |
|  | $142 \times \frac{275}{493}=$ | = 79.21 | OR | $275 \times \frac{142}{493}=79.21$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | $\begin{aligned} & \mathrm{AO} 2 \\ & \mathrm{AO} 1 \end{aligned}$ | Or any equivalent correct method |
| (iii) | Chi-squared contributions |  |  |  |  |  |  |
|  | Age (years) |  |  |  |  |  |  |
|  | Parent knows password | 13 | 14 | ${ }^{15}$ |  |  |  |
|  | Yes | 2.779 | 0.175 | 1.180 |  |  |  |
|  | No | 2.203 | 0.139 | 0.935 | A1 | AO1 | FT 'their observed values' |
| (iv) | 2 degrees of freedom from (3-1) $\times(2-1)$ |  |  |  | B1 | AO1 |  |
| (v) | Since $p$-value $<0.05$, Reject $\mathrm{H}_{0}$ |  |  |  | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | $\begin{aligned} & \mathrm{AO} 1 \\ & \mathrm{AO} 2 \end{aligned}$ | B1 for $<0.05$ <br> B1 for Reject $\mathrm{H}_{0}$ |
|  | Strong evidence to suggest there is an association between parents knowing their child's social media passwords and age |  |  |  | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | $\begin{aligned} & \mathrm{AO} 2 \\ & \mathrm{AO} 3 \end{aligned}$ | B1 for strong evidence B 1 for relating back to hypothesis |
| (b) | Largest contribution for 13-year-olds especially for yes It seems more parents than expected know passwords for their 13-year-old children. |  |  |  | E1 <br> E1 [12] | $\begin{aligned} & \mathrm{AO} 2 \\ & \mathrm{AO} 2 \end{aligned}$ |  |

